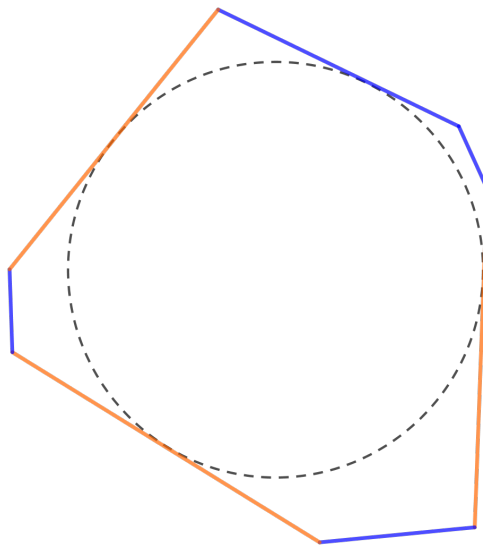




PROBLEM OF THE WEEK #4  
(Spring 2023)

Let  $P$  be a polygon whose edges have been painted either blue or orange, in such a way that the edges next to an orange edge are always blue. (However, blue edges may be next to each other.) Prove: if the sum of the lengths of the orange edges is greater than the sum of the lengths of the blue edges, then you can't inscribe a circle in  $P$  (that is, no circle is tangent to every edge of  $P$ ).



[Please fully explain your answer.]

Email solutions to [kwonmi@uwplatt.edu](mailto:kwonmi@uwplatt.edu) by 2:00pm on Wednesday, February 22, 2023.

Every week, the best solution submitted earns a \$10 Platteville gift certificate; the top scorer each semester also wins a cash award. Good luck!  
You can always see the Problem of the Week (and complete rules) online at:

<http://uwpmath.weebly.com/>