



PROBLEM OF THE WEEK #10
(Spring 2022)

Let $x = \frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2}$, where n is a positive integer. Since x is a rational number, it has a repeating or terminating decimal form. Show that x has a repeating (non-terminating) decimal, but the repeating part doesn't start immediately after the decimal point. For example, when $n = 4$, we get $x = \frac{37}{60} = 0.616666\dots$, in which the "61" that follows the decimal point doesn't repeat.

[Please fully explain your answer.]

Email solutions to kwonmi@uwplatt.edu by 2:00pm on Wednesday, April 13, 2022.

Every week, the best solution submitted earns a \$10 Platteville gift certificate; the top scorer each semester also wins a cash award. Good luck!

You can always see the Problem of the Week (and complete rules) online at:

<http://uwpmath.weebly.com/>