



PROBLEM OF THE WEEK #1  
 (Spring 2020)

Prove that the grid of numbers shown below is not a proper sudoku puzzle, because it does not have a unique solution.

		4			7		3	
6		5						
	7	1		4	9			
			9	1		4	7	5
4	5	7		3	6			
			1	6		5	9	
						1		3
	9		4			7		

**Solution:**

*Proof.* No 2s and no 8s appear in the grid, so, if any solution exists, then you can also find a different solution by switching the locations of the 2s and the 8s. □

*Remark.* In fact, there are exactly four solutions to this ill-posed sudoku, which are suggested by the grids below.

9	<sup>28</sup>	4	6	5	7	<sup>28</sup>	3	1
6	3	5	<sup>28</sup>	<sup>28</sup>	1	9	4	7
<sup>28</sup>	7	1	3	4	9	6	5	<sup>28</sup>
3	6	<sup>28</sup>	9	1	<sup>28</sup>	4	7	5
<sup>28</sup>	1	9	5	7	4	3	6	<sup>28</sup>
4	5	7	<sup>28</sup>	3	6	<sup>28</sup>	1	9
7	<sup>28</sup>	<sup>28</sup>	1	6	3	5	9	4
5	4	6	7	9	<sup>28</sup>	1	<sup>28</sup>	3
1	9	3	4	<sup>28</sup>	5	7	<sup>28</sup>	6

9	<sup>28</sup>	4	6	5	7	<sup>28</sup>	3	1
6	3	5	<sup>28</sup>	<sup>28</sup>	1	9	4	7
<sup>28</sup>	7	1	3	4	9	6	5	<sup>28</sup>
3	6	<sup>28</sup>	9	1	<sup>28</sup>	4	7	5
<sup>28</sup>	1	9	5	7	4	3	<sup>28</sup>	6
4	5	7	<sup>28</sup>	3	6	<sup>28</sup>	1	9
7	<sup>28</sup>	<sup>28</sup>	1	6	3	5	9	4
5	4	6	7	9	<sup>28</sup>	1	<sup>28</sup>	3
1	9	3	4	<sup>28</sup>	5	7	6	<sup>28</sup>

**Source:** Suggested by: "Sudoku." *Wisconsin State Journal*, 2 November 2019, B5 (which was a proper sudoku).