Problem of the Week \#7
(Fall 2022)

If $N$ dots can be arranged in rows to form an equilateral triangle, with one dot in the first row, two dots in the second row, and in general $k$ dots in the $k^{\text {th }}$ row, then $N$ is called a triangular number. For instance, ten is a triangular number (ten dots form a 4-row triangle).
In base 9 , ten is written 11. Show that every number whose base-9 digits are all 1 s is triangular.
[Please fully explain your answer.]
Email solutions to kwonmi@uwplatt.edu by 4:00pm on Wednesday, November 2, 2022.

Every week, the best solution submitted earns a $\$ 10$ Platteville gift certificate; the top scorer each semester also wins a cash award. Good luck!
You can always see the Problem of the Week (and complete rules) online at:

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http://uwpmath.weebly.com/
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