



UNIVERSITY OF WISCONSIN  
**PLATTEVILLE**  
DEPARTMENT OF MATHEMATICS

PROBLEM OF THE WEEK #5  
(Fall 2017)

- (a) Let  $f$  and  $g$  be functions for which  $f \circ g = g$  and  $g \circ f = f$ . Prove:  $f \circ f = f$  and  $g \circ g = g$ .
- (b) Find distinct functions  $f$  and  $g$  with domain  $\mathbb{R}$  for which  $f \circ g = g$  and  $g \circ f = f$ .

[Please fully explain your answer.]

Solutions should be submitted to Cinda Furry, in Gardner Hall 435, by 4:00 P.M. on Wednesday, October 18, 2017.

Every week, the best solution submitted earns a \$10 Platteville gift certificate; the top scorer each semester also wins a cash award. Good luck!

You can always see the Problem of the Week (and complete rules) online at:

<http://uwpmath.weebly.com/>